

List of Languages

List of languages:

1. $U = \{\langle M, x \rangle \mid \text{Turing machine } M \text{ accepts input } x\}$ is undecidable but recognizable.
2. $\overline{U} = \{\langle M, x \rangle \mid \text{Turing machine } M \text{ does not accept input } x\}$ is unrecognizable.
3. $D = \{\langle M \rangle \mid \text{Turing machine } M \text{ does not accept } \langle M \rangle\}$ is unrecognizable.
4. $\overline{D} = \{\langle M \rangle \mid \text{Turing machine } M \text{ accepts } \langle M \rangle\}$ is undecidable but recognizable.
5. $H = \{\langle M, x \rangle \mid \text{Turing machine } M \text{ halts on input } x\}$ is undecidable but recognizable.
6. $\overline{H} = \{\langle M, x \rangle \mid \text{Turing machine } M \text{ doesn't halt on input } x\}$ is unrecognizable.
7. $E = \{\langle M \rangle \mid \text{Turing machine } M \text{ accepts no input}\}$ is unrecognizable.
8. $\overline{E} = \{\langle M \rangle \mid \text{Turing machine } M \text{ accepts some input}\}$ is undecidable but recognizable.
9. $REG = \{\langle M \rangle \mid \text{Turing machine } M \text{ accepts regular languages}\}$ is undecidable.
10. $\overline{REG} = \{\langle M \rangle \mid \text{Turing machine } M \text{ does not accept regular languages}\}$ is undecidable.
11. $HET = \{\langle M \rangle \mid \text{TM } M \text{ halts on empty tape}\}$ is undecidable but recognizable.
12. $\overline{HET} = \{\langle M \rangle \mid \text{TM } M \text{ doesn't halt on empty tape}\}$ is unrecognizable.
13. $ODD = \{\langle M \rangle \mid L(M) \text{ is finite and } |L(M)| \text{ is odd}\}$ is not recognizable.
14. $\overline{ODD} = \{\langle M \rangle \mid L(M) \text{ is infinite or } |L(M)| \text{ is even}\}$ is not recognizable.
15. $FIN = \{\langle M \rangle \mid L(M) \text{ is finite}\}$ is not recognizable.
16. $INF = \{\langle M \rangle \mid L(M) \text{ is infinite}\}$ is not recognizable. ($INF = \overline{FIN}$)
17. $EQUIV = \{\langle M1, M2 \rangle \mid L(M1) = L(M2)\}$ is not recognizable.
18. $\overline{EQUIV} = \{\langle M1, M2 \rangle \mid L(M1) \neq L(M2)\}$ is not recognizable.
19. $SUBSET = \{\langle M1, M2 \rangle \mid L(M1) \subseteq L(M2)\}$ is not recognizable.
20. $\overline{SUBSET} = \{\langle M1, M2 \rangle \mid L(M1) \not\subseteq L(M2)\}$ is not recognizable.

Here is a picture showing if each of the above languages is decidable, recognizable or unrecognizable.

